

Chapter 15: Oscillations

- periodic motion: motion that repeats itself at regular time intervals
- period (T): time to complete one oscillation (seconds)
- frequency (ν): number of oscillations per unit time (Hz, one cycle/second)
- simple harmonic motion: oscillations in which the acceleration (+ net force) of a system is proportional to the displacement and acts in the opposite direction of the displacement ex/ a spring on a frictionless surface with mass m attached
- equilibrium position: position where the spring is neither stretched nor compressed (typically $x = 0$)
- With vertical spring motion, the force of gravity acts to change the equilibrium position of the spring. Both F_g and F_s act on the spring.
- Total mechanical energy of a horizontal spring system = $U + K = \frac{1}{2}kx^2 + \frac{1}{2}mv^2 = \frac{1}{2}kA^2$
- stable equilibrium point = forces on either side of eq point act to return an object to a stable eq point
- unstable equilibrium = forces on either side of eq point act to move object away from unstable eq point
- physical characteristics of springs
 - if cut in half, the spring constant on each new spring doubles (series combination)
 - if the length is doubled, the new spring constant will halve
 - if two springs are placed next to each other, the new spring constant will be $k_1 + k_2$ (parallel combination)

Equations

$$F = -kx$$

spring force spring constant displacement

$$U = \frac{1}{2}k(\Delta x)^2$$

spring potential energy

- $kx = \max$
 - $kx = m \frac{d^2x}{dt^2}$

$$\frac{d^2x}{dt^2} + \left(\frac{k}{m}\right)x = 0$$

characteristic equation of simple harmonic motion

$$X = A \cos(\omega t + \phi)$$

amplitude (max displacement) rad/sec

phase shift: when starting at a $\theta \neq 0$, shifts θ coordinate

so $X_{\max} = A$

where $v = -\omega A \sin(\omega t + \phi) \rightarrow v_{\max} = \omega A$ (occurs at equilibrium)

and $a = -\omega^2 A \cos(\omega t + \phi) \rightarrow a_{\max} = \omega^2 A$ (occurs at extremes)

remembering that $\omega = 2\pi\nu$ and $T = \frac{1}{\nu}$

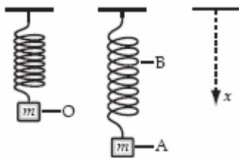
$$\omega = \sqrt{\frac{k}{m}}$$

$$E = \frac{1}{2}kA^2$$

total mechanical energy amplitude (max displacement)

Practice Problems

- (easy) A light flashes every 8.00×10^{-5} seconds. What is the frequency of the flashes?
- (medium) When an 80.0-kg man stands on a pogo stick, the spring is compressed 0.120 m .
 - What is the spring constant?
 - Will the spring be compressed more when he hops down the road?
- (hard) A weight of mass m is at rest at O when suspended from a spring, as shown. When it is pulled down and released, it oscillates between positions A and B .
 - At what point does the rate of change of its momentum have the greatest magnitude?
 - Where is the point of greatest gravitational potential energy?
 - Where is the point of least elastic potential energy?



Solutions

1. $T = 8 \times 10^{-5}$
 $f = \frac{1}{T} = \frac{1}{8 \times 10^{-5}} = 12,500 \text{ Hz}$

2. a) $F = ma = -k\Delta x$
 $mg = -k\Delta x$
 $(80)(9.8) = -k(0.120)$
 $k = 6533$

b) Yes. When the man is at his lowest point in his hopping the spring will be compressed the most.

3. a) A and B
b) B
c) O